

2.6 Modeling with Inequalities

Examples:

1. Five times a number, decreased by 24, is greater than 3 times the number. Find the possible numbers.

$$\begin{aligned} \text{let } x &= \text{number} \\ 5x - 24 &> 3x \\ -24 &> 3x - 5x \\ -24 &> -2x \\ \frac{-24}{-2} &< x \\ 12 &< x \end{aligned}$$

The number is greater than 12.

2. Sara has \$53.50 in her pocket and wants to purchase shirts at a sale price of \$14.95 each. How many shirts can she buy?

$$\text{let } x = \# \text{ of shirts } (14.95)$$

$$14.95x \leq 53.50$$

$$x \leq \frac{53.50}{14.95}$$

$$x \leq 3 \frac{173}{299}$$

3 Shirts

3. The length of a rectangle is 5 cm more than its width. The perimeter of the rectangle is at least 66 cm. Find the minimum measures of the length and width.

$$\begin{aligned} \text{let } x &= \text{width} \\ x + 5 &= \text{length} \\ 2l + 2w &= P \\ 2(x + 5) + 2(x) &\geq 66 \\ 2x + 10 + 2x &\geq 66 \\ 4x + 20 &\geq 66 - 10 \\ 4x &\geq 46 \\ x &\geq \frac{46}{4} \\ x &\geq 11.5 \end{aligned}$$

$$\begin{array}{|l} P \geq 66 \text{ cm} \\ x \end{array}$$

$$\begin{aligned} x &= 14 \\ x + 5 &= 19 \end{aligned}$$

width = 14 cm
length = 19 cm

4. Mrs. Scott decided that she would spend no more than \$120 to buy a jacket and a skirt. If the price of the jacket was \$20 more than 3 times the price of the skirt, find the highest possible price of the skirt.

$$\begin{aligned} \text{let } x &= \text{price of skirt} \\ 3x + 20 &= \text{price of jacket} \end{aligned}$$

$$x + (3x + 20) \leq 120$$

$$x + 3x + 20 \leq 120$$

$$4x \leq 120 - 20$$

$$4x \leq 100$$

$$x \leq \frac{100}{4}$$

$$x \leq 25$$

The highest price of the skirt is \$25.

HOMEWORK

Worksheet - HW 2.6 Modeling with Inequalities